

# WORKSHOP ON GRAPH THEORY AND ITS APPLICATIONS - IX

**Date :** November 1-2, 2019

**Place:** IMBM Seminar Room, Boğaziçi University South Campus

**Participation is free, please register on our web page**

<https://bilmuh.gtu.edu.tr/~dgozupek/wgt2019/>

## PROGRAM

### November 1, 2019, Friday

**10.00-12.15 (with a coffee break):** *On 1-well-covered graphs and unimodality conjectures*

Vadim Levit (Ariel University, Israel)

Abstract:

A graph is *well-covered* if all its maximal independent sets are of the same size (Plummer, 1970). A well-covered graph is *1-well-covered* if the deletion of any one vertex leaves a graph, which is well-covered as well (Staples, 1975).

A graph  $G$  belongs to class  $\mathbf{W}_n$  if every  $n$  pairwise disjoint independent sets in  $G$  are included in  $n$  pairwise disjoint maximum independent sets (Staples, 1975). Clearly,  $\mathbf{W}_1$  is the family of all well-covered graphs. It turns out that  $G \in \mathbf{W}_2$  if and only if it is a 1-well-covered graph without isolated vertices.

We show that deleting a shedding vertex does not change the maximum size of a maximal independent set including a given independent set. Specifically, for well-covered graphs, it means that the vertex  $v$  is shedding if and only if  $G - v$  is well-covered. In addition, we provide new characterizations of 1-well-covered graphs and study unimodality properties of their independence polynomials.

**14.00-17.00:** Contributed talks

### November 2, 2019, Saturday

**10.00-12.15 (with a coffee break):** *On the generalised colouring numbers*

Sebastian Siebertz (University of Bremen, Germany)

Abstract:

The generalised colouring numbers  $wcol_r$ ,  $col_r$ , and  $adm_r$  were introduced by Kierstead and Yang, and by Dvořák as generalisations of the usual colouring number of graphs. They have found many applications in graph theory, and in particular, they play a key role in the theory of bounded expansion and nowhere dense graphs introduced by Nešetřil and Ossona de Mendez. We overview combinatorial and algorithmic applications of the generalised colouring numbers, emphasising new developments in this area.

**14.00-17.00:** Contributed talks

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